

Unraveling the Reaction Mechanism for Nickel-Catalyzed Oxidative Dehydrogenation of Ethane by DFT: The C–H Bond Activation Step and Its Following Pathways

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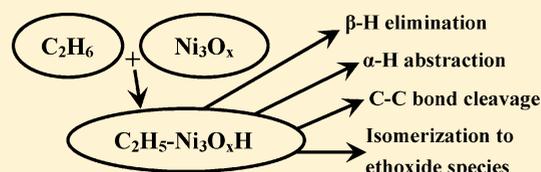
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S Supporting Information

ABSTRACT: Understanding the reaction mechanism for oxidative dehydrogenation (ODH) of alkanes, especially the key intermediate(s) that generates alkene is essential for designing good ODH catalysts. To unravel the mechanisms for Ni-based oxide-catalyzed ODH reactions, we investigated the reactions of C₂H₆ with Ni₃O_x (x = 1, 2, 3) clusters by density functional calculations. For Ni₃O₃, three pathways were examined for the C–H bond activation step, and the one with concerted mechanism

undergoing at two sites is the most favorable pathway, producing an ethylnickel species. Then, four reaction pathways, namely, β-H elimination, α-H abstraction, C–C bond cleavage, and isomerization to an ethoxide species, with 11 reaction channels, were examined to understand the behavior of this ethylnickel species. The selectivity of C₂H₄ (S_{C2}) for this reaction was calculated based on the relative rates of these four pathways. Similar investigations were carried out on the reactions of Ni₃O₂ and Ni₃O₁ clusters with C₂H₆. The calculated S_{C2} increases from ~37 to over 99% with decreasing x value in Ni₃O_x.



1. INTRODUCTION

Selective conversions of light alkanes to molecules with functional groups are of great industrial and fundamental interest, especially nowadays because the oil price remains at a high level and oil depletion in three to five decades is widely expected. Oxidative dehydrogenation (ODH) of light (C₂–C₄) alkanes provides an attractive alternative to the present methods for production of alkenes.^{1–3} The key problem for the industrial application of ODH is still the unavailability of catalyst presenting desired selectivity to alkene with high conversion of alkane. Great efforts for seeking such catalyst have been made for several decades.¹ However, the reaction mechanisms for catalytic ODH reactions are still elusive in the literature.^{2,3} Most ODH works emphasize in catalytic reaction tests, whereas many fewer concerns have been taken in reaction mechanism,^{4–10} especially on the molecular level.¹¹ This is partially due to the short lifetime of the surface intermediate(s) involved during the oxidation of alkane by metal oxides and the reoxidation of reduced metal site(s) by oxidants. Several key questions about the detailed ODH mechanism are poorly understood, such as: (Q1) what is the primary intermediate(s) after the C–H bond activation of alkane on a catalyst,^{2,3} (Q2) what is the reaction behavior of this intermediate(s), (Q3) how does the structure of active site effect the type and the reaction behavior of the intermediate(s), and (Q4) how does one increase the concentration of the active site(s), which favors the intermediate(s) kinetically leading to high selectivity of alkene on a catalyst?

Obviously the answers to the above questions are essential for designing good ODH catalysts. Quantum chemical, especially density functional theory (DFT)^{12–21} calculation, provides powerful tools for understanding a reaction system on the molecular level. Presently, in most of the DFT studies dealing with the ODH reaction,^{14–16,19,20} the models for catalyst are single-crystal surfaces. However, a huge gap exists between the well-defined single-crystal surfaces and the surfaces of most solid catalysts, in that typically the latter contain ill-defined metal/metal oxide clusters, the size of which range from subnanometer to ~50 nm. Therefore, using metal oxide cluster models seems to be more plausible than using single-crystal models for the active sites in heterogeneous catalysis,^{21–23} which could be even more right when dealing with the active sites of around or less than 1 nm (subnanometer). Subnanometer materials were found to possess catalytic properties not observed in their large-size analogues, and subnanometer catalysts may have attractive properties in catalysis.^{24,25} DFT calculations using cluster models will help researchers better understand the field of catalysis with subnanometer catalysts.

This work aims at seeking the answers for questions Q1 and Q2 proposed in the first paragraph for Ni-catalyzed ODH reaction of ethane (ODHE). Although V^{26–28} and Mo^{4,29,30} are the most extensively studied metals for ODH, in the recent

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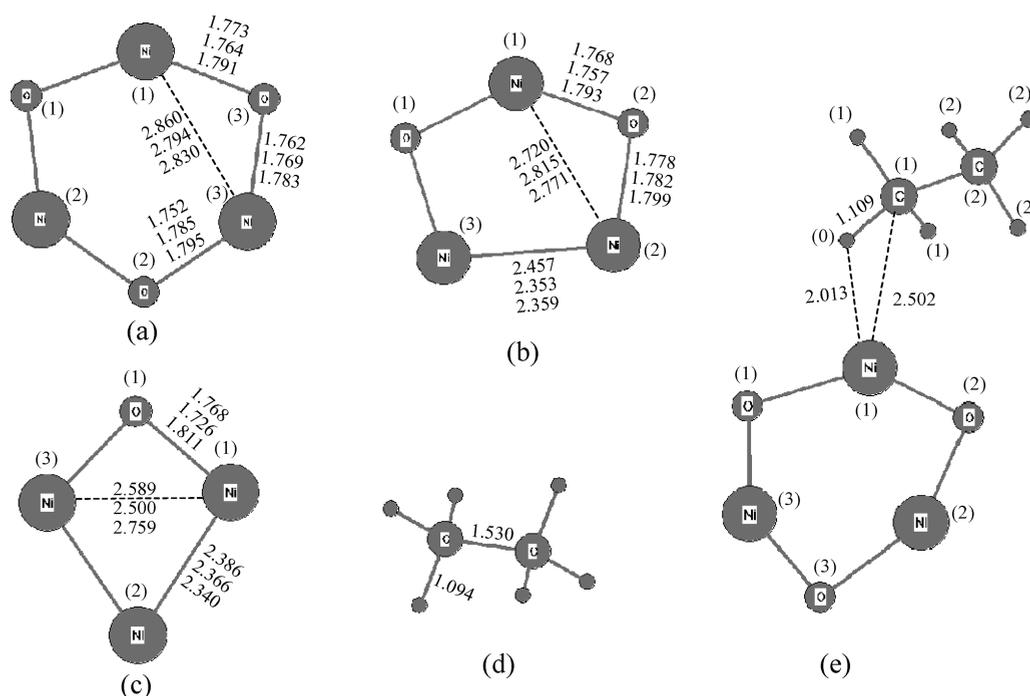


Figure 1. Ni_3O_3 (a), Ni_3O_2 (b), and Ni_3O_1 (c) models, C_2H_6 molecule (d), and the reactant complex of a C_2H_6 molecule with a Ni_3O_3 cluster in heptet state (e). Key distances are indicated in angstroms. The three stacking numbers from top to bottom are the distances in triplet, quindruplet, and heptet states, respectively. Geometry optimizations were done on the B3LYP/BS1 level, which will not be indicated hereafter in this Article.

73 years Ni-based catalysts were found to present good yield of
 74 ethylene^{31–41} in the ODHE reactions, and some reports for
 75 using Ni catalysts for ODH of propane^{42,43} can also be seen in
 76 the literature. For example, ODHE catalyzed by NiO-loaded
 77 high-surface-area MgO was examined by Nakamura and
 78 coworkers,³⁹ and a C_2H_6 conversion of 68.8% and a C_2H_4
 79 selectivity of 52.8% were achieved at 600 °C. Ni-loaded H–Y
 80 catalyst giving a productivity of C_2H_4 over 1 $\text{g}_{\text{C}_2\text{H}_6/\text{cat}}^{-1} \text{h}^{-1}$ at 600
 81 °C was reported by our group.³⁶ Catalyst giving a productivity
 82 of C_2H_4 smaller than this value is unlikely to be interested by
 83 industrial investors.¹

84 In this work, DFT calculations were carried out to
 85 characterize the potential energy surfaces (PESs) of the
 86 reactions between Ni_3O_x ($x = 1, 2, 3$) clusters and C_2H_6 to
 87 understand the key steps in Ni-catalyzed ODH reactions. The
 88 aim of this work is to shed light on the fate of an alkane
 89 molecule when encountered with metal oxide by examining
 90 different pathways of the C–H bond activation step (denoted
 91 as the first step in this Article) and the fate of the intermediate
 92 generated from the first step by examination of different
 93 pathways of bond cleavage for this intermediate (denoted as the
 94 second step). We found the reaction rate of the β -H
 95 elimination pathway relative to the sum of rates for all
 96 pathways in the second step, which determines the product
 97 selectivity of ethylene (S_{C_2}) for a certain reaction. S_{C_2} can be
 98 associated with the initial selectivity of ethylene (S_0) in a
 99 catalytic ODHE reaction. Our results provide a new insight into
 100 the intermediate(s) involved in transition metal-catalyzed
 101 oxidation of light alkanes. A discussion on how to design
 102 good ODH catalysts is given based on the conclusions.

2. COMPUTATIONAL METHODS AND THE MODELS OF Ni_3O_x CLUSTERS

104 DFT calculations were performed by employing the hybrid
 105 B3LYP^{44–46} exchange and correlation functionals to explore

the PESs of the reaction between C_2H_6 and Ni_3O_x ($x = 1, 2, 3$)
 106 clusters. B3LYP is known to provide a good description of the
 107 PES for the transition-metal oxide clusters.^{21,47} All of the PESs
 108 were examined by optimizing geometries in the energy
 109 minimums for the reactants, the intermediates, and the
 110 products and the first-order saddle points for transition states
 111 using the Gaussian 03 program suite.⁴⁸ Frequency analyses
 112 were performed to confirm energy minimums and first-order
 113 saddle points as well as to obtain the zero-point corrected
 114 energies (ZPEs), entropies, and free energies (at 298.15,
 115 823.15, and 873.15 K) of the optimized geometries. The
 116 temperature mainly concerned is 873.15 K. The 6-311G**
 117 basis set was used for all C, H, O atoms, and the Stuttgart basis
 118 set was used for the Ni atoms. Five component d functions
 119 were employed in the calculations. These basis sets are denoted
 120 as BS1 in this Article.
 121

The results reported in our previous papers^{35,36} indicate that
 122 several first-row transition-metal-loaded Y zeolites (M/Y) may
 123 exist in quite small clusters because no features relating to M
 124 can be observed on the X-ray diffraction patterns, whereas the
 125 elemental analysis shows significant metal loadings. The ex situ
 126 EXAFS (extended X-ray absorption fine structure) spectro-
 127 scopic study shows that the Ni components in Ni/HY can be
 128 represented as NiO·Ni,³⁶ when Ni/HY is exposed to a fuel-rich
 129 reaction mixture of ethane, O_2 , and He. Therefore, it is
 130 reasonable to expect that the active sites on Ni-loaded zeolite
 131 catalyst are small NiO·Ni_{*i*} clusters. Therefore, the Ni_3O_x ($x = 1,$
 132 2, 3) clusters were used to model the nickel oxide clusters on
 133 the catalytic supports such as zeolites. The optimized
 134 geometries of Ni_3O_3 , Ni_3O_2 , and Ni_3O_1 are presented in
 135 Figure 1a–c.
 136

Metal oxide clusters may have different spin multiplicities
 137 close in energy.²¹ For the reactions involving the Ni_3O_3 and
 138 Ni_3O_2 clusters, only the reaction pathways with triplet,
 139 quindruplet and heptet states will be presented in this paper,
 140

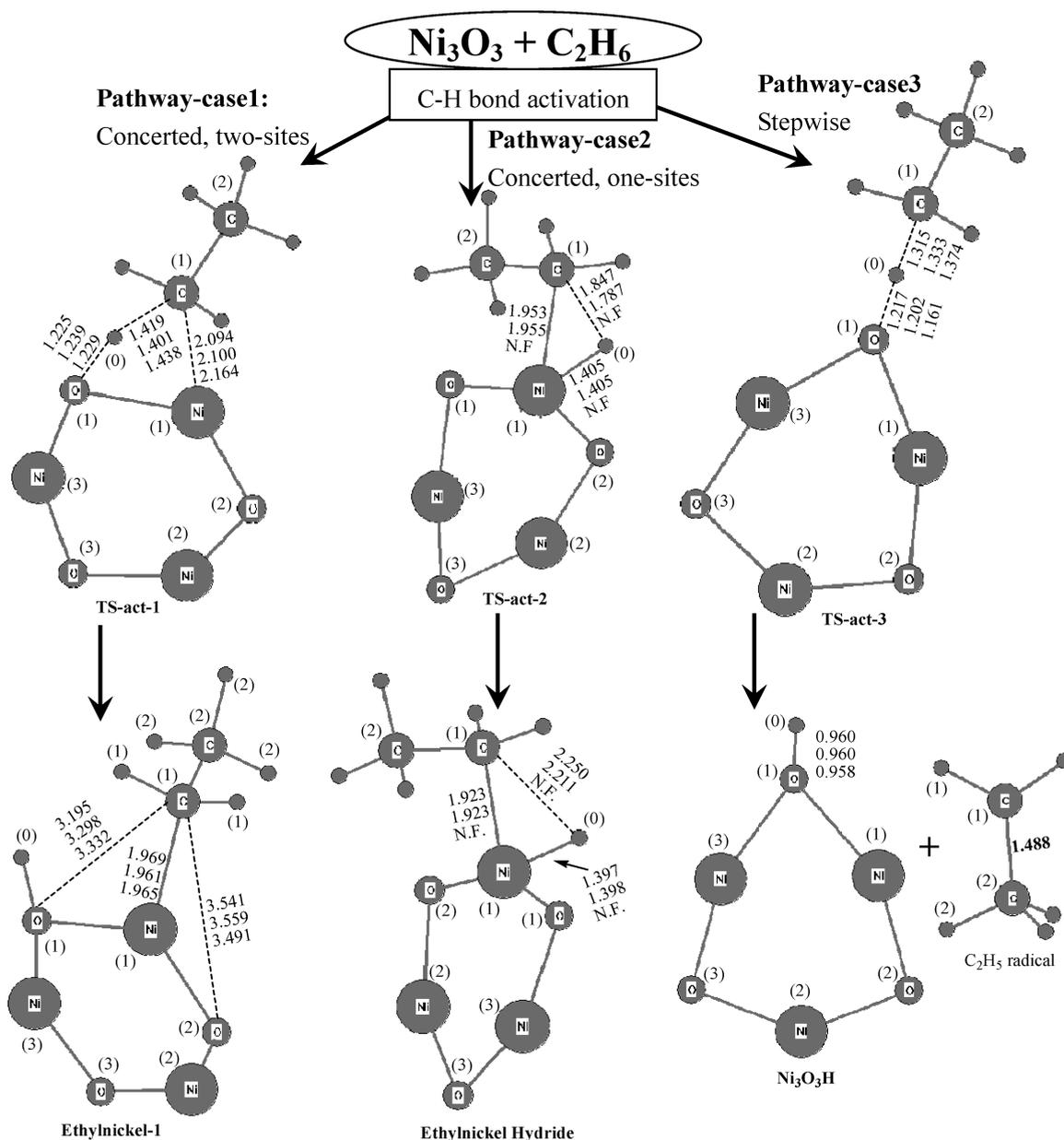


Figure 2. Optimized geometries for the transition states and product complexes or separated products for three pathways examined in the C–H bond activation step for the reaction of Ni₃O₃ with C₂H₆. Key distances are indicated in angstroms. The three stacking numbers from top to bottom are the distances in triplet, quadruplet, and heptet states, respectively. “N.F.” stands for “not found”.

141 since the energies of the relating species with singlet and nonet
142 states are much higher than those with triplet, quadruplet and
143 heptet states. For the reactions involving the Ni₃O₁ cluster, only
144 the reaction pathways on triplet and quadruplet PESs will be
145 reported because the energies of the relating species with
146 singlet, heptet, and nonet states are much higher than those
147 with triplet and quadruplet states.

3. RESULTS AND DISCUSSION

148 **3.1. First Step of Ni₃O₃ Case: C–H Bond Activation of**
149 **C₂H₆.** The C–H bond activation was extensively studied for
150 either homogeneous^{49–51} or heterogeneous catalysis.^{22,23,52}
151 The main target of this section is to understand question Q1, as
152 described in the Introduction, for the cases of using nickel oxide
153 as ODH catalyst.

For C₂H₆ reacting with Ni₃O₃, heptet Ni₃O₃ + C₂H₆ was 154
chosen as the starting material (SM), and the energy or free 155
energy of SM was selected as the reference. Molecular 156
adsorption of C₂H₆ on heptet Ni₃O₃ was first examined by 157
locating the local energy minimum when a C₂H₆ molecule 158
approaches the Ni₃O₃ cluster. The energy minimum appears at 159
the C(1)⋯Ni(1) distance of ~2.5 Å (Figure 1e). The energy 160
change of adsorption calculated, for example, for the case of 161
heptet Ni₃O₃ cluster, is –2.9 kcal/mol, which is close to –2.5 162
kcal/mol for the adsorption of ethane on V₂O₅(001) surface.¹⁵ 163
The entropy loss for the formation of this reactant complex 164
from the separated reactants is 75.3 J·mol^{–1}·K^{–1} at 298.15 K and 165
113.9 J·mol^{–1}·K^{–1} at 873.15 K. Considered that the OHDE 166
reaction typically undergoes at the temperature range of 600– 167
1000 K, this entropy loss results in a more stable state in the gas 168
phase than being adsorbed on the metal oxide surface. 169

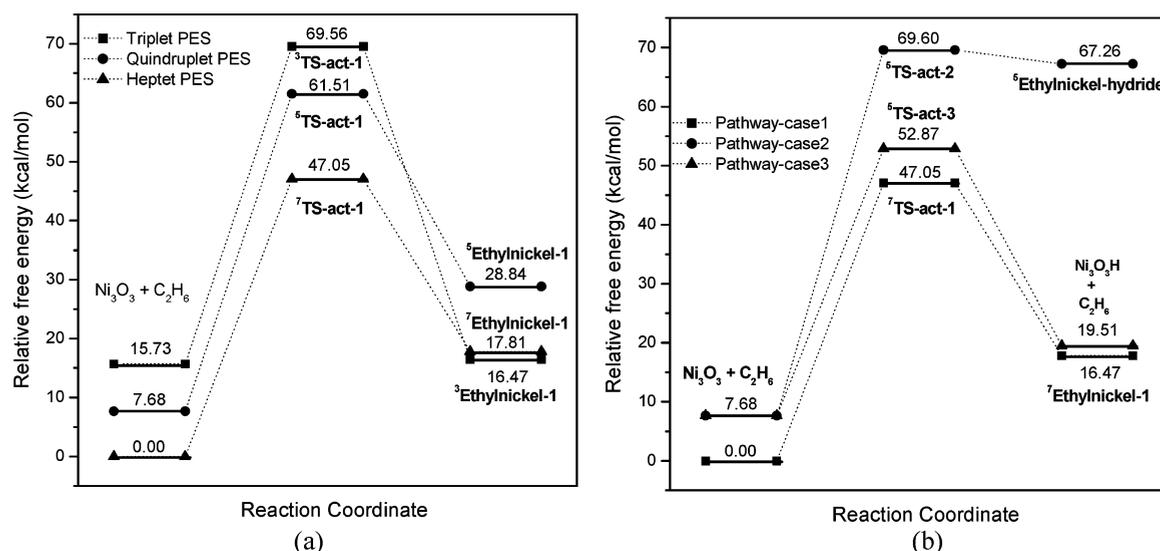


Figure 3. Relative free energy (at 873.15 K) profiles for the C–H bond activation step in C₂H₆ reacting with Ni₃O₃. The free energy of heptet Ni₃O₃ + C₂H₆ is the reference. (a) Free-energy profiles for **pathway-case1** on triplet, quindruplet, and heptet PESs. (b) Three pathways with their lowest free energy of activations.

170 Therefore, it is reasonable to conclude that the activation of C–
 171 H bond in C₂H₆ is not precursor-mediated.¹⁵ It has been
 172 pointed out by some researchers⁵³ that a more accurate method
 173 to calculate the adsorption energy is to use the correlation
 174 function including the van der Waals force instead of B3LYP
 175 for the adsorption of alkane on metallic surface. However,
 176 considering the case that the typical temperature for desorption
 177 of alkane from metallic surface is under 200 K,⁵⁴ the above
 178 conclusion is still plausible.

179 The C–H bond activation step of alkanes on metal oxides
 180 may undergo with different mechanisms,²² which can be
 181 divided into two categories: concerted and stepwise mecha-
 182 nisms. In the concerted mechanism, the cleavage of the C–H
 183 bond is accompanied by the formation of two new bonds. For
 184 the case of C–H bond activation on Ni₃O₃, the C(1) and H(0)
 185 atoms (Figure 1e) may form new bonds with one O site, with
 186 one Ni site, or with two sites. Although many attempts were
 187 performed by considering all possible combinations, the
 188 transition-state structures of only two reaction pathways,
 189 namely, **pathway-case1** and **pathway-case2**, were found for
 190 the concerted mechanism. (See Figure 2.) For **pathway-case1**,
 191 the C(1)–H(0) bond cleavage is accompanied by the
 192 formation of the H(0)–O(1) and C(1)–Ni(1) bonds, which
 193 can be seen from the changes of atom distances from SM to the
 194 transition state, **TS-act-1**, and to the product, **Ethynickel-1**
 195 species, as shown in Figure 1a,d and the left two panels of
 196 Figure 2. For **pathway-case2** (Figure 2), both of the C(1) and
 197 H(0) atoms attack the Ni(1) site, and the C(1)–Ni(1) and
 198 H(0)–Ni(1) bonds are formed in the product of the C–H
 199 bond activation step.

200 For the stepwise mechanism, only one pathway (**pathway-**
 201 **case3** in Figure 2) was found, where the cleavage of C(1)–
 202 H(0) bond is accompanied by the formation of H(0)–O(1)
 203 bond. Different from the cases of **pathway-case1** and **pathway-**
 204 **case2**, two separated products are produced: a Ni₃O₃H and an
 205 ethyl radical. The combination of this two separated products
 206 to form a further product complex was not examined.

207 The free energy of activation (ΔG^\ddagger) needed for different
 208 pathways may be different, and if one pathway has an obviously
 209 lower ΔG^\ddagger than other pathways have then this pathway can

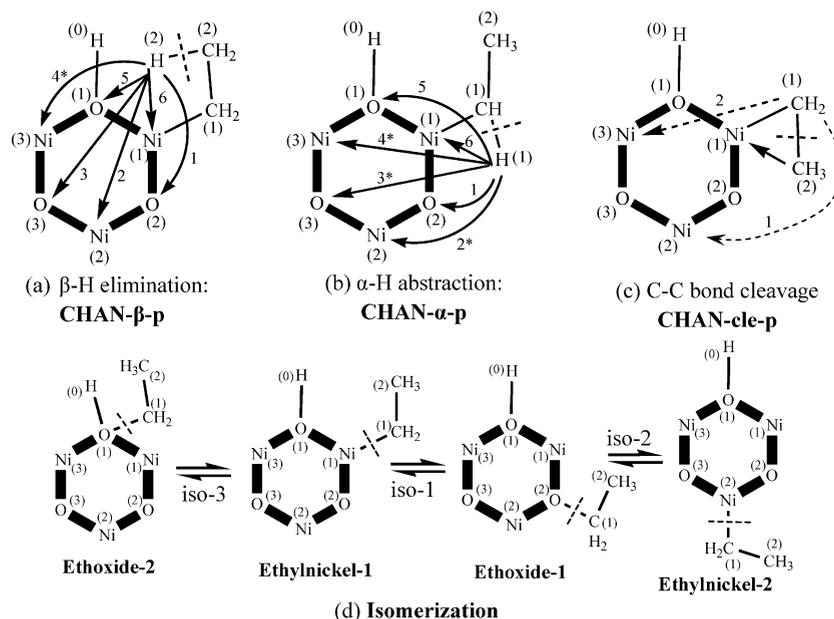
the dominant one for the C–H bond activation step. Figure 3a 210 B
 211 shows the relative free-energy profiles for **pathway-case1** with
 212 triplet, quindruplet, and heptet states, respectively. ΔG^\ddagger for the
 213 heptet state (47.1 kcal/mol at 873.15 K) is the lowest in the
 214 three spin multiplicities for **pathway-case1**. Figure 3b shows
 215 that the lowest ΔG^\ddagger for **pathway-case2** is 69.6 kcal/mol, and
 216 the lowest ΔG^\ddagger for **pathway-case3** is 52.9 kcal/mol with all
 217 spin multiplicities examined. These data bring the answers of
 218 the following two important questions for the C–H bond
 219 activation step: (1) what is the contribution of a certain spin
 220 multiplicity to a given pathway and (2) what is the contribution
 221 of a certain pathway to the overall C–H bond activation step?

In general, for two parallel pathways that share a same
 222 reactant or if the reactants of which are easier to change to each
 223 other than go to the transition states, the relative reaction rate
 224 of these two pathways can be determined by the Boltzmann
 225 distribution⁵⁵ of their corresponding transition states, which
 226 can be written as 227

$$r_2/r_1 = \exp\left(\frac{G_{TS1} - G_{TS2}}{RT}\right) \quad (1)$$

where G_{TS} is the free energy of a transition state relative to an
 228 arbitrary reference. By applying the data in Figure 3a to eq 1,
 229 one can obtain that for **pathway-case1** $r_{\text{triplet}}/r_{\text{heptet}} = 2.3 \times 10^{-6}$
 230 and $r_{\text{quindruplet}}/r_{\text{heptet}} = 2.4 \times 10^{-4}$ at 873.15 K. So for the
 231 **pathway-case1**, the reaction undergoes with the heptet state
 232 dominantly, and the contribution of other spin multiplicities
 233 can be discarded. Similar conclusions can be drawn for
 234 **pathway-case2** and **pathway-case3**; that is, only one spin
 235 multiplicity dominates each pathway, and the contributions of
 236 other spin multiplicities are trivial. 237

Some readers may argue about the validity of the above
 238 conclusion from eq 1 when concerning that sometimes the
 239 conversion between different spin multiplicities for a species
 240 may be “spin-forbidden”; therefore, the reaction rates with
 241 different spin multiplicities should be calculated independently.
 242 To understand how spin state influences the above conclusions
 243 made from eq 1, we calculated the energies of Ni₃O₃ with
 244 different multiplicities with a same geometry. It was found that 245

Scheme 1. Four Reaction Pathways Including Different Channels Examined for Ethylnickel-1^a

^aNumber in the parentheses represents the atomic label. The number near the arrow represents the channel number (p value) for a certain pathway in panels a–c, where the number with a star represents the corresponding channel that was not found in this work. In panel d, iso-1 and iso-3 are the two isomerization channels for **Ethylnickel-1**, and iso-1 and iso-2 are the two isomerization channels for **Ethoxide-1**.

246 for the same Ni_3O_3 geometry (optimized geometry with heptet
247 state, see Figure 1a), the free-energy difference between a
248 heptet and a quadruplet state ($G_{\text{heptet}} - G_{\text{quadruplet}}$) is 11.3
249 kcal/mol. The $G_{\text{heptet}} - G_{\text{triplet}}$ and $G_{\text{quadruplet}} - G_{\text{triplet}}$ values are
250 19.4 and 8.1 kcal/mol, respectively. The data obtained in this
251 way are definitely larger than the exact value of the minimum
252 energy needed for spin conversions, obtaining which requires a
253 full scan of PESs. However, they are still enough to conclude
254 that the spin conversion between different multiplicities is
255 much faster than the C–H bond activation step because the
256 energy needed for the spin conversion (<20 kcal/mol) is much
257 smaller than that needed for the C–H bond activation (with
258 the least of 47.1 kcal/mol). This meets the precondition of eq
259 1. Therefore, in our reaction systems, nearly only one spin
260 multiplicity contributes to a certain pathway, and the relative
261 reaction rate of two certain pathways can be calculated from the
262 corresponding lowest free energy of transition states without
263 considering what the spin multiplicities are.

264 Using the data in Figure 3b and eq 1, one can obtain that
265 $k_{\text{case2}}/k_{\text{case1}}$ is 8.8×10^{-6} and $k_{\text{case3}}/k_{\text{case1}} = 0.035$. That is to say,
266 for the C–H bond activation step, the contribution of the
267 radical mechanism is little, and that of the pathway where the C
268 and H atoms attack a same site is even less. As can be seen in
269 the lower-left panel of Figure 2, an ethylnickel species (denoted
270 as $\text{C}_2\text{H}_5\text{-Ni}_3\text{O}_3\text{H}$, simply **Ethylnickel-1** in this Article) can be
271 identified in the product of the main pathway (pathway-case1)
272 for the C–H bond activation step. Therefore, it can be
273 anticipated that the reaction behavior of **Ethylnickel-1**
274 determines the initial selectivities of different oxidation
275 products for the whole oxidation reaction of ethane with nickel
276 oxides. A systematic investigation of four reaction pathways
277 with several reaction channels was carried out for **Ethylnickel-**
278 **1**, and the results are presented in Section 3.2.

279 **3.2. Second Step of Ni_3O_3 Case: Reaction Behavior of**
280 **Ethylnickel-1.** Compared with the C–H bond activation step
281 for hydrocarbons, the reaction behavior of the intermediate

produced from the C–H bond activation step was less
studied.^{12–21} The main goal for this section is to understand
question Q2 in the Introduction for the cases of using nickel
oxide as ODH catalyst.

The possible reaction pathways of **Ethylnickel-1** can be
elucidated by inspection of the number of types of chemical
bond in its $\text{Ni-C}_2\text{H}_5$ moiety. There are four types of chemical
bond, that is, the α -C–H [C(1)–H(1)], β -C–H [C(2)–
H(2)], C–C [C(1)–C(2)], and Ni–C [C(1)–Ni(1)] bonds
in the $\text{Ni-C}_2\text{H}_5$ moiety of **Ethylnickel-1**. (See the lower-left
panel of Figure 2 or Scheme 1.) Because the chemical reaction
involves bond cleavage, the cleavages of these bonds
correspond to the following four reaction pathways, respec-
tively: α -H abstraction, β -H elimination, C–C bond cleavage,
and isomerization. (Going back to the starting materials will not
be considered here.) All four reaction pathways of **Ethylnickel-**
1 may undergo with different reaction channels, considering
that the detached part may go to different sites. The possible
reaction channels for the β -H elimination, α -H abstraction, and
C–C cleavage pathways are illustrated in Scheme 1a–c, and the
two reaction channels of the isomerization pathway are
illustrated in Scheme 1d. For example, in Scheme 1a, the β -H
atom [H(2) as indicated] may go to six sites, leading to six
possible reaction channels for the β -H elimination pathway.
However, for some reaction channels, the transition states and
products were not found despite several attempts.

3.2.1. β -H Elimination Pathway. For the β -H elimination
pathway, the reaction channels are denoted as CHAN- β - p ,
where $p = 1–6$, as indicated in Scheme 1a. The corresponding
transition states are denoted as TS- β - p . CHAN- β -4 was not
found, which could account for the less positively charged of
the Ni(3) compared with the other Ni site because the ethyl
moiety is going to be oxidized when H elimination undergoes.
This is verified from the charge analysis. The transition states
and products for all other channels are presented in Figure 4.

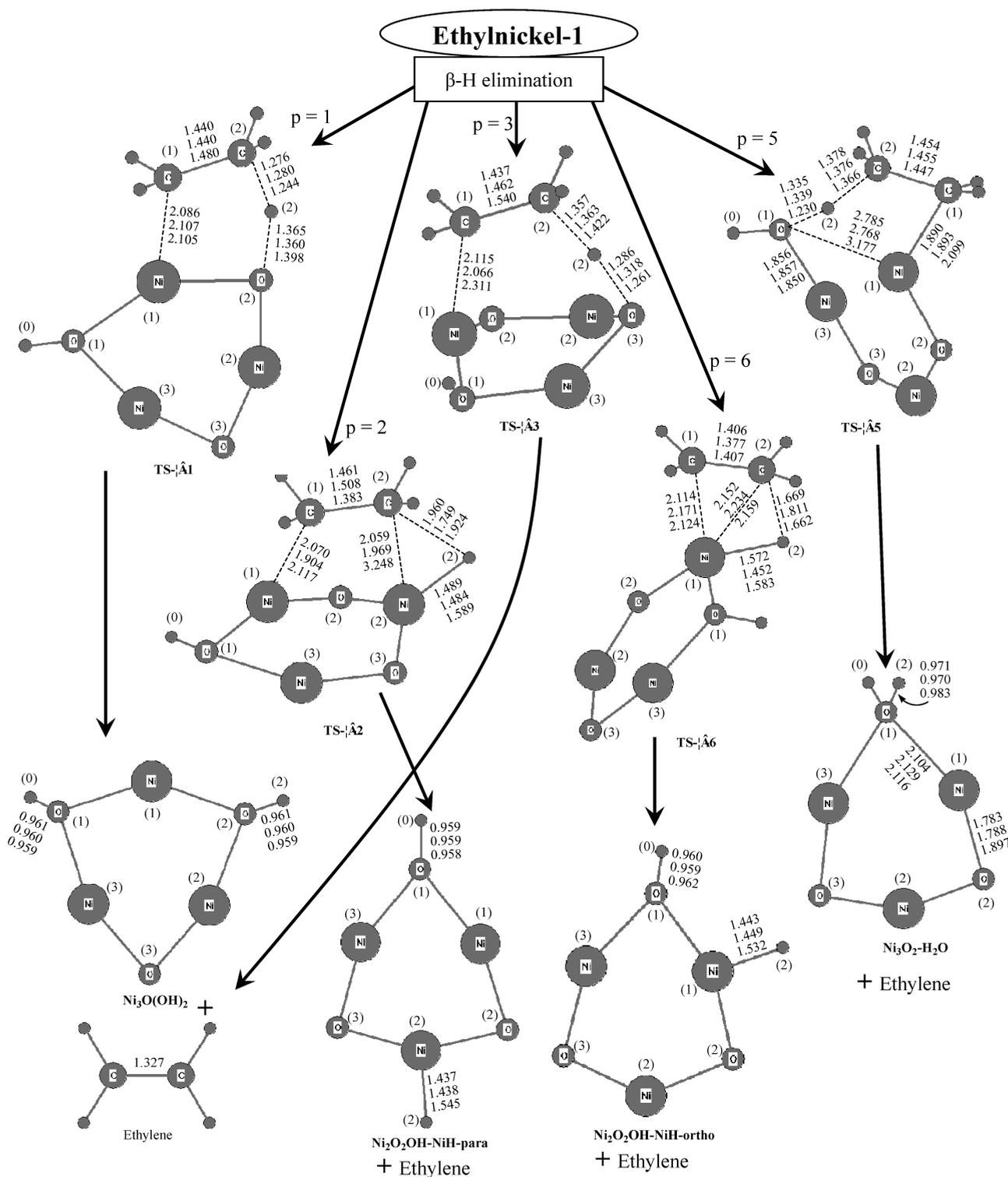


Figure 4. Optimized geometries for the transition states and products for five reaction channels examined for the β-H elimination pathway of Ethynickel-1. Key distances are indicated in angstroms. The three stacking numbers are the distances in triplet, quindruplet, and heptet states, respectively. See Scheme 1a as well.

317 Comparison of the transition state and product structures of
 318 **CHAN-β-1** with that of **Ethynickel-1**, a clear process of β-H
 319 elimination can be identified,¹⁵ with the detachment of C(1)
 320 from Ni(1) atom, the detachment of H(2) from C(2) atom, the
 321 approaching of H(2) to O(2) atom, and shortening of the
 322 C(1)–C(2) bond from a single to double bond length, at the
 323 same time. For example, C(2)⋯H(2) distance increased from

1.091 Å in **Ethynickel-1** to 1.280 Å in TS-β-1 in quindruplet
 324 (or ⁵TS-β-1) state, and they are totally detached as in separated
 325 products. In **CHAN-β-2**, a trigonal C(2)⋯H(2)⋯Ni(2)
 326 structure can be seen in the transition-state structure (TS-β-
 327 2). The C(2)⋯H(2) distance in TS-β-2 is larger than that in
 328 TS-β-1, implicating that the detachment of H(2) from C(2) is
 329 more difficult in **CHAN-β-2** than in **CHAN-β-1**. This 330

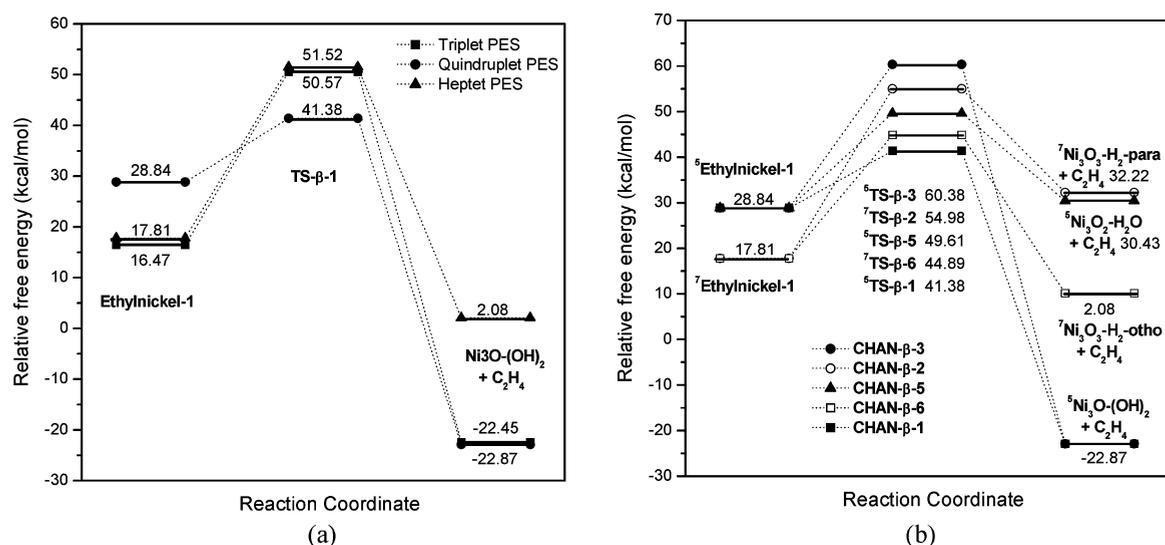


Figure 5. Relative free energy (at 873.15 K) profiles for the β -H elimination pathway of **Ethylnickel-1**. The free energy of heptet Ni₃O₃ + C₂H₆ is the reference. (a) Free-energy profiles for **CHAN- β -1** on triplet, quintuplet, and heptet PESs. (b) Five reaction channels with their lowest free energy of activations.

hypothesis is supported in the free-energy profiles shown in Figure 5. Product complexes for **CHAN- β -1** and **CHAN- β -2** are the molecular adsorption of an ethylene molecule on different Ni₃O₃H₂ structures. The separated C₂H₄ and Ni₃O₃H₂ were found to be more favorable in free energy than the product complexes. Therefore, in all of the reaction channels for the β -H elimination pathway, the structures of product complexes will not be presented in this Article.

The transition state and product structures for **CHAN- β -3** are similar to those for **CHAN- β -1**, as can be seen in Figure 4. In the transition-state structure (**TS- β -5**) for **CHAN- β -5**, the approaching of the H(2) atom to O(1) atom leads to the detachment of O(1) from Ni(1) at the same time. The Ni₃O₃H₂ product for **CHAN- β -5** is the adsorption of a water molecule on the Ni₃O₂ cluster. In **TS- β -6** for **CHAN- β -6**, a four-membered-ring feature of [C(1)⋯C(2)⋯H(2)⋯Ni(1)] can be seen, similar to the local structure reported for the dehydrogenation of ethane on GaO⁺ ion.⁴⁷

Similar to the questions raised in Section 3.1, now it is important to evaluate the contribution of different spin multiplicity to the rate of a certain reaction channel and the contribution of different reaction channel to the rate of a certain pathway. Figure 5a presents the free-energy profiles for **CHAN- β -1** with the spin multiplicity of triplet, quintuplet, and heptet. Applying the data in Figure 5a to eq 1, one can obtain that $k_{\text{triplet}}/k_{\text{quintuplet}} = 0.0052$, and $k_{\text{heptet}}/k_{\text{quintuplet}} = 0.0029$ at 873.15 K, indicating that the triplet and heptet states have trivial contributions to the reaction channel **CHAN- β -1**, which is most favorable to undergo in the quintuplet state.

Similar to the discussion in Section 3.1, because of the spin conversion issue, the above results calculated by using eq 1 are correct only if the energy needed for spin conversion is lower than that needed for the reaction itself. So the energies of heptet and quintuplet **Ethylnickel-1** with the geometry optimized in triplet state were calculated, and the free energies needed for spin conversions between different spin states were found to be no larger than 12.1 kcal/mol. This is much smaller than the free energy of activation for any reaction channels in the β -H elimination pathway (Figure 5b). For all reaction channels examined in this work, only one certain spin

multiplicity among triplet, quintuplet, and heptet has major contribution to a certain reaction channel. Therefore, the structural and energetic information are presented only for the spin multiplicities with the lowest free energy of the transition state, hereafter in this Article.

The free-energy profile depicted in Figure 5b shows that among all five reaction channels examined for the β -H elimination pathway the most favorable one is **CHAN- β -1**. That is, the β -H atom is most favorable to go to the O(1) site rather than other sites. For the two channels where the β -H atom goes to a Ni site, **CHAN- β -2** and **CHAN- β -6**, the latter is more favorable. That is, compared with other Ni sites, the β -H atom is relatively easy to go to the nearest Ni site [Ni(1)]. Using eq 1, one can obtain that $k_{\beta-6}/k_{\beta-1}$ is 0.132, $k_{\beta-5}/k_{\beta-1}$ is 0.0087, and the relative rates of other channels over the rate of **CHAN- β -1** are even much smaller. That is, over 88% of the β -H atoms go to the O(1) site, and $\sim 11.5\%$ of the β -H atoms go to the Ni(1) site, and the contributions of other channels are negligible.

By inspection of Figure 5b, it was found that **CHAN- β -1** and **CHAN- β -3** are mildly exothermic, **CHAN- β -6** is slightly endothermic, and **CHAN- β -2** and **CHAN- β -3** are mildly endothermic. This indicates that it is thermodynamically favorable for H to go to “bare” O site (such as O(2) or O(3)) rather than other sites.

3.2.2. α -H Abstraction Pathway. Although there are possibly six sites for the α -H atom to go to as indicated in Scheme 1b (**CHAN- α -p**), the transition-state structures of only three reaction channels, that is, **CHAN- α -1**, **CHAN- α -5**, and **CHAN- α -6**, were found. The other three reaction channels were not found, maybe because the Ni(2), O(3), and Ni(3) site are too far for the α -H atom compared with the Ni(1), O(1), and O(2) sites. **TS- α -p** and **PC- α -p** are denoted as the transition states and product complexes for **CHAN- α -p** (where $p = 1,5,6$), and their optimized geometries are presented in Figure 6. By inspection of the geometrical parameters shown in Figure 6, it can be seen that for **CHAN- α -1** and **CHAN- α -5**, the detachment of the H(1) atom from C(1) atom is accompanied by the decrease in the C(1)–Ni(1) bond length as well as the H(1)⋯O distance. For **CHAN- α -6**, where the α -H

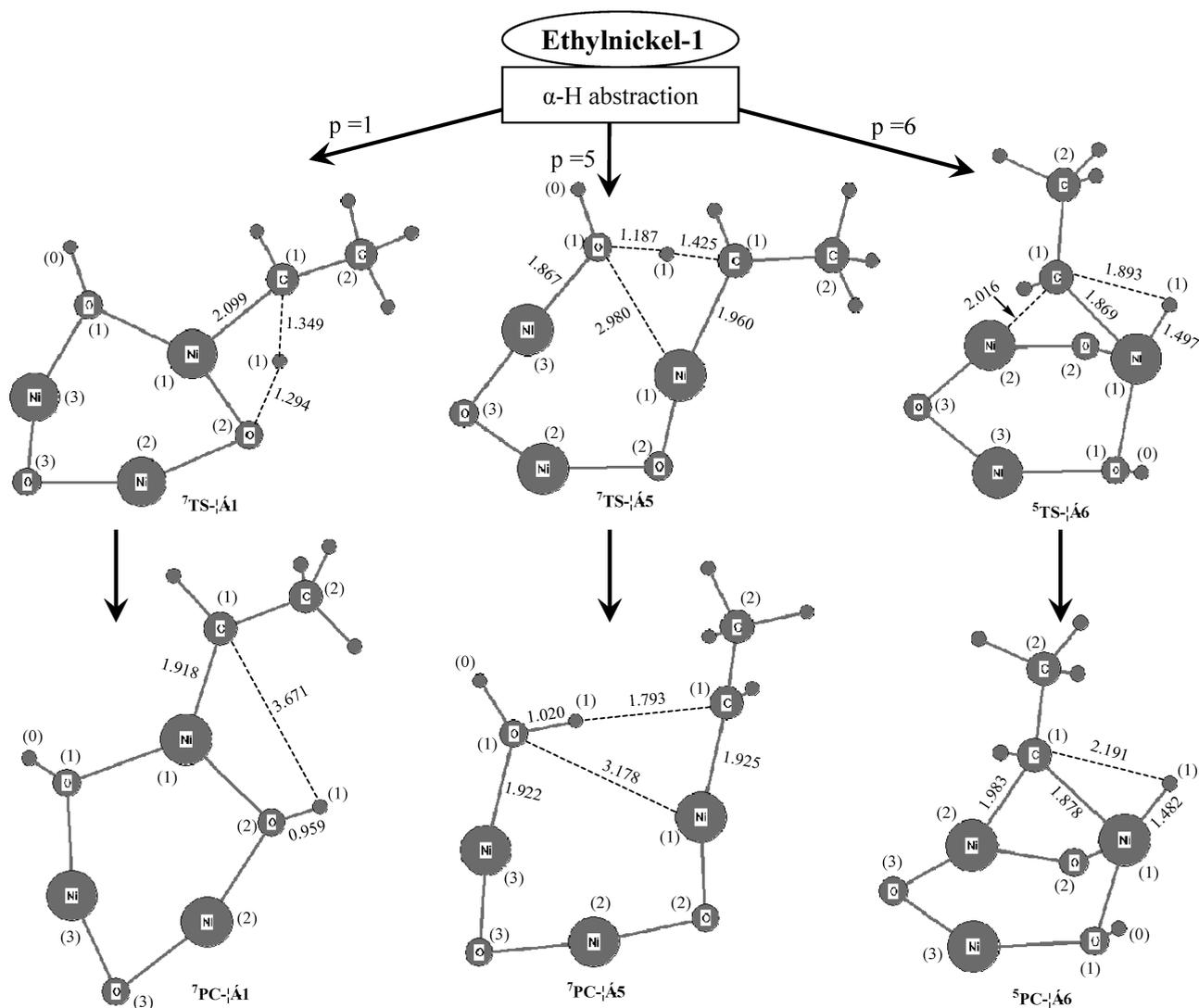


Figure 6. Optimized geometries for the transition states and product complexes for three reaction channels examined for the α -H abstraction pathway of Ethynickel-1. Key distances are indicated in angstroms. The upper-left number of the notation of each structure is the spin multiplicity. See Scheme 1b as well.

411 H atom is abstracted by the Ni(1) site, the C(1)⋯H(1)
 412 distance in the transition state (TS- α -6) is much larger than
 413 that in TS- α -1 or TS- α -2, implicating that the abstraction of
 414 the α -H atom by the α -Ni atom is much more difficult than that
 415 by the nearby O atoms. This hypothesis is supported by Figure
 416 7a, which depicts the relative free-energy profiles of these α -H
 417 abstraction reaction channels.

418 As can be seen in Figure 7a, the free energy of TS- α -6 is
 419 higher than that of TS- α -5 for ~ 19 kcal/mol, whereas that of
 420 TS- α -1 is rather close to that of TS- α -5. Using eq 1, one can
 421 obtain $k_{\alpha-6}/k_{\alpha-5} = 2.1 \times 10^{-5}$ and $k_{\alpha-1}/k_{\alpha-5} = 0.37$. These data
 422 mean that the α -H atom may go to either one of the nearest O
 423 atom for the α -H abstraction pathway.

424 **3.2.4. C–C Bond Cleavage Pathway.** Detachment of the
 425 methyl [C(2)H₃] group from the methylene [C(1)H₂] moiety
 426 in the ethyl group leads to the C–C bond cleavage pathways
 427 for Ethynickel-1, and in this work only two reaction channels,
 428 as indicated in Scheme 1c, were found. In both of reaction
 429 channels, the C–C bond cleavage pathway undergoes only at
 430 the nearest Ni [Ni(1)] site. The C(1)H₂ moiety has to find
 431 another site to form a new bond during the detachment of the

432 methyl group. The channel where a new bond formed between
 433 C(1) and Ni(2) is denoted as CHAN-cle-1, and the one where
 434 a new bond formed from C(1) and Ni(3) is denoted as
 435 CHAN-cle-2, as indicated in Scheme 1c. Figure 8 presents the
 436 optimized geometries of the transition states (TS-cle- p , $p =$
 437 1,2) and product complexes (PC-cle- p) involved in CHAN-cle-
 438 p , and Figure 7b depicts the relative free-energy profiles for
 439 these two reaction channels. A local trigonal structure of
 440 C(1)⋯C(2)⋯Ni(1) in TS-cle- p with the C⋯C distance of
 441 ~ 2.1 Å, which is very similar to the reductive elimination step
 442 of Ni(terpyridine)-catalyzed cross-coupling reactions.⁵⁶ This
 443 reductive elimination step (forming C–C bond) can be
 444 considered to be the reverse step of C–C bond cleavage. As
 445 can be seen in Figure 7b, these two reaction channels have a
 446 close free energy of activation, and the PCs are both highly
 447 endothermic.

448 **3.2.4. Isomerization Pathway between an Ethynickel and**
 449 **an Ethoxide Species.** An important issue for transition-metal-
 450 catalyzed oxidation of hydrocarbon is the type of primary
 451 species generated from the C–H bond activation step and the
 452 type of species directly responsible for the initial product

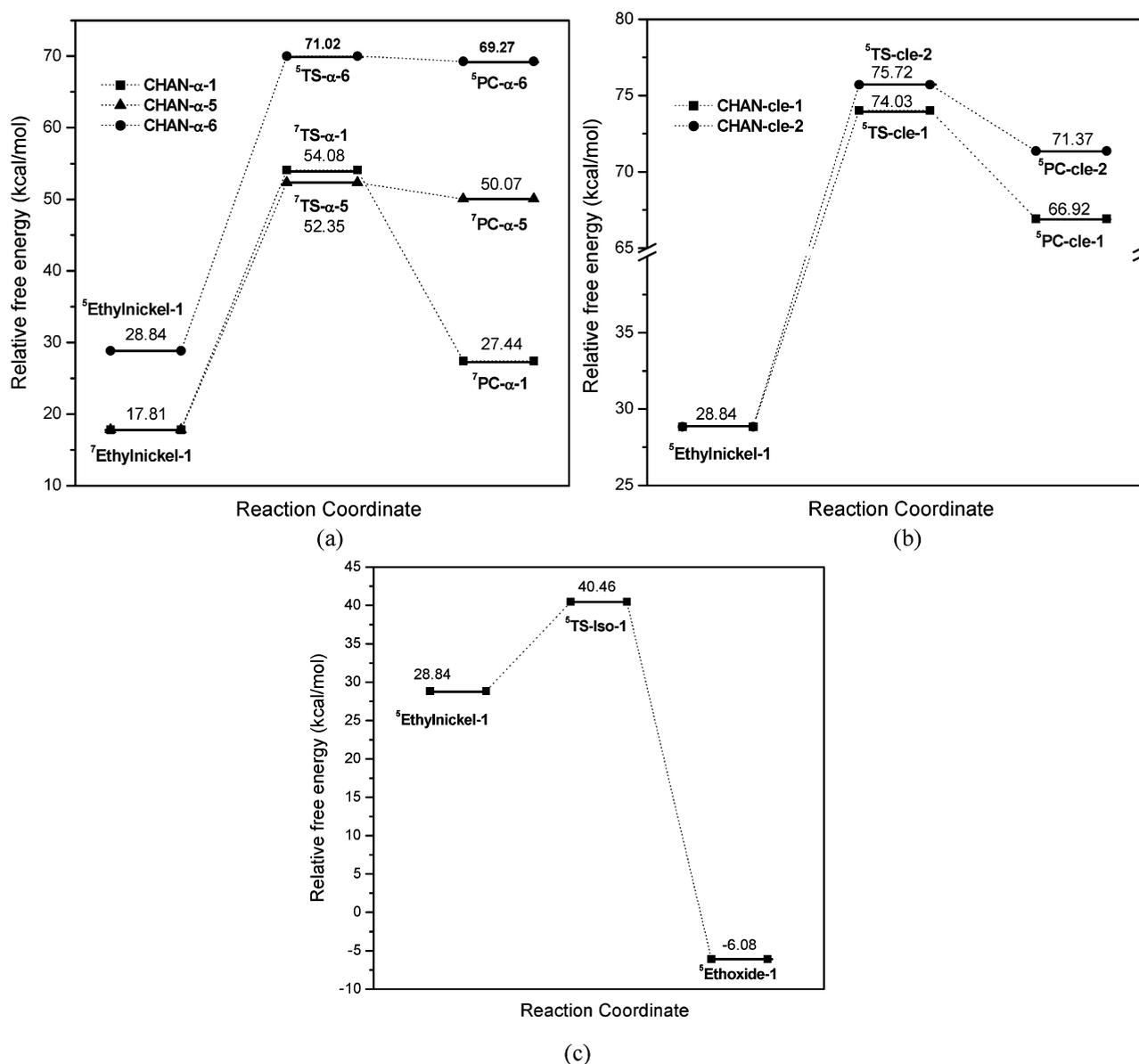


Figure 7. Relative free energy (at 873.15 K) profiles for (a) the three channels of the α -H abstraction pathway of **Ethylnickel-1**, (b) the two channels of the C-C bond cleavage pathway of **Ethylnickel-1**, and (c) the isomerization of **Ethylnickel-1** to **Ethoxide-1**. The free energy of heptet $\text{Ni}_3\text{O}_3 + \text{C}_2\text{H}_6$ is the reference.

453 selectivity observed in experiment. Because the alkyl group can
 454 be bounded to a metal site to form an alkylmetal or bounded to
 455 an O site to form a metal alkoxide, many concerns have been
 456 taken to the issue for whether alkylmetal or metal alkoxide is
 457 the key intermediate responsible for the initial selectivity.^{2,3,57,58}
 458 Because of the short lifetime of the suggested intermediate(s),
 459 presently there are no spectroscopic data from which the
 460 structure of intermediate can be unequivocally determined.
 461 Busca and coworkers⁵⁸ have used IR to study the surface
 462 species on the Mn_3O_4 , Co_3O_4 , and MgCr_2O_4 catalysts when
 463 exposed to a reaction feed of propane and O_2 , and they
 464 suggested that the intermediates of metal propoxides be
 465 plausible.

466 In this work, efforts have been taken on understanding how
 467 easily the above two intermediates isomerize to each other.
 468 Scheme 1d shows two reaction channels (**iso-1** and **iso-3**) for
 469 the isomerization pathway of **Ethylnickel-1** and two channels
 470 for **Ethoxide-1** (**iso-2** and the reverse of **iso-1**). The first

pictorial panel in Figure 9 shows the transition-state (**TS-iso-1**)
 structure for transforming **Ethylnickel-1** to **Ethoxide-1**, and the
 second panel in Figure 9 shows the structure of the **Ethoxide-1**.
 The **iso-3** channel where **Ethylnickel-1** transforms to
Ethoxide-2 was not found, which could be accounted for less
 positive charge of the O(1) site than that of other O sites.
 The free energy of **TS-iso-1** with quadruplet state is 40.5 kcal/
 mol (Figure 7c), and the free energy of activation for the
 isomerization step is 22.6 kcal/mol at 873 K. This free energy
 of activation corresponds to a first-order reaction rate constant
 of $3.9 \times 10^7 \text{ s}^{-1}$ using gas-phase model or a half-lifetime of $1.8 \times$
 10^{-8} s . Even at room temperature, the free energy of activation
 for **Ethylnickel-1** to isomerize to **Ethoxide-1** is 18.2 kcal/mol,
 which corresponds to a half-life time of only 2.5 s. **Ethoxide-1**
 is more stable than **ethylnickel-1** by 26.1 kcal/mol lower in
 energy, respectively. The above energetic data indicate that in a
 typical alkane oxidation system where the reaction temperature
 is usually over 600 K, it is very difficult to capture alkylmetal

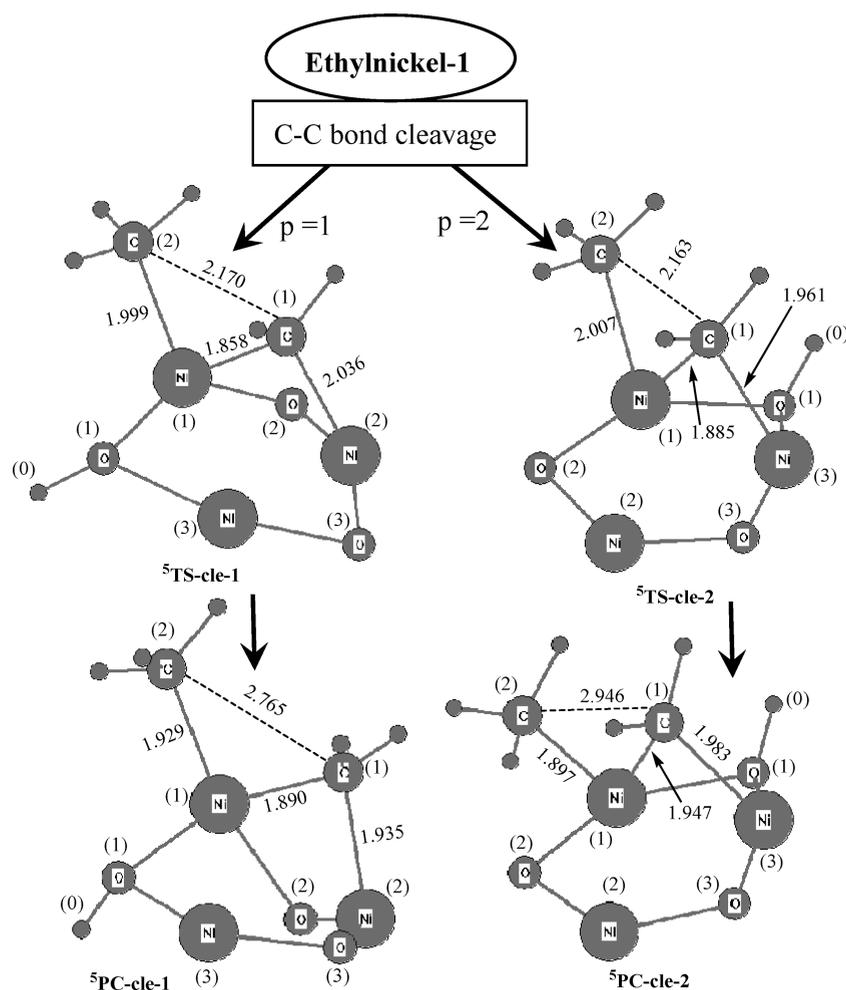


Figure 8. Optimized geometries for the transition states and product complexes for the two reaction channels examined for the C–C bond cleavage pathway of **Ethylnickel-1**. Key distances are indicated in angstroms. The upper-left number of the notation of each structure is the spin multiplicity. See Scheme 1c as well.

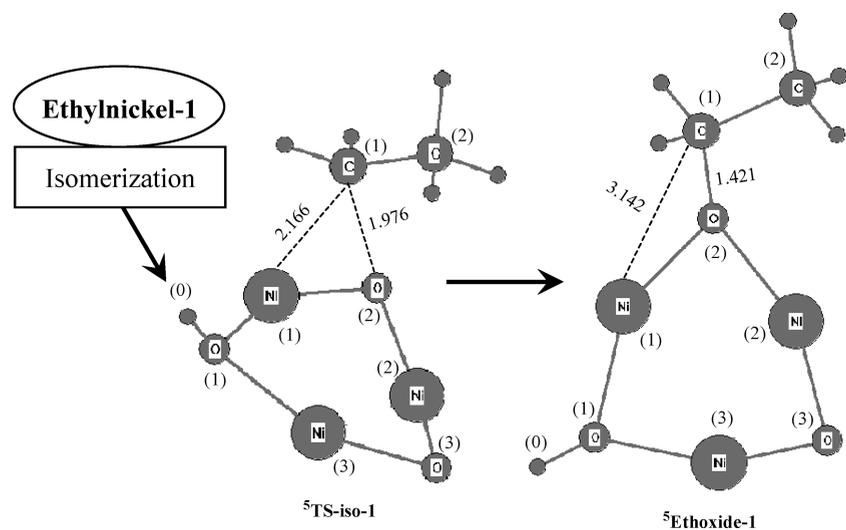
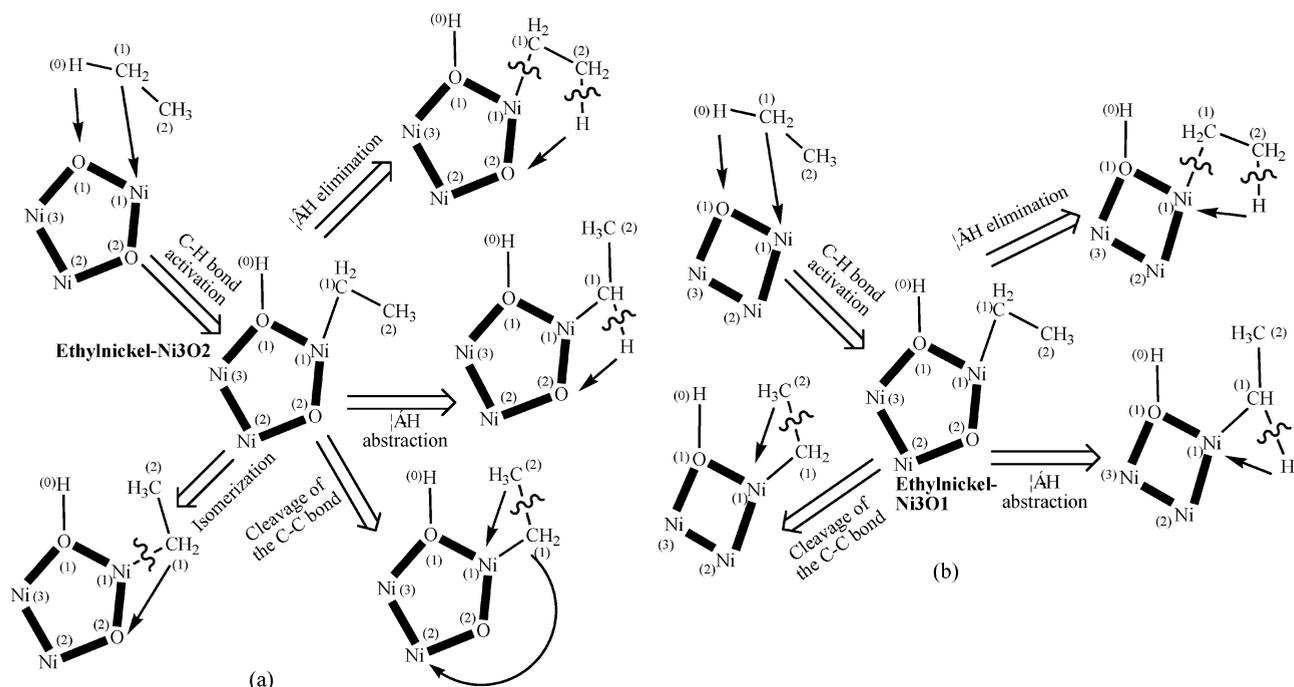


Figure 9. Optimized geometries for the transition states and product for the isomerization of **Ethylnickel-1** to **Ethoxide-1**. Key distances are indicated in angstroms. The upper-left number of the name of each structure is the spin multiplicity. See Scheme 1d as well.

489 species using in situ spectroscopic tools due to its short lifetime.
 490 If an alkylmetal species can be formed at room or even lower
 491 temperatures, then it would be feasible to observe it before
 492 transforming to other species.

3.2.5. Reaction Pathways of Ethoxide-1 Species. Because
 493 the isomerization of **Ethylnickel-1** to **Ethoxide-1** is rather facile
 494 and thermodynamically favorable, it is important to explore the
 495 reaction behaviors of **Ethoxide-1** to better understand the 496

Scheme 2^a

^a(a) Schematic diagrams for the C–H bond activation step and the four reaction pathways in the following step for the case of C₂H₆ reacting with Ni₃O₂ cluster. (b) Schematic diagrams for the C–H bond activation step and the three reaction pathways in the following step for the case of C₂H₆ reacting with Ni₃O₁ cluster. All of the optimized geometries involved in these two reactions are presented in Figure 3S for (a) and Figure 4S for (b) in the Supporting Information.

497 initial product selectivity. For **Ethoxide-1**, besides the β -H
 498 elimination, α -H abstraction, and C–C bond cleavage path-
 499 ways, there are two isomerization pathways (reverse of **iso-1** to
 500 produce **Ethynickel-1** and **iso-2** to produce **Ethynickel-2** as
 501 indicated in Scheme 1d). To emphasize the main points of this
 502 work, we present here only the reaction channel with the lowest
 503 free energy for each reaction pathway. The optimized
 504 geometries for the two isomerization pathways and their
 505 corresponding free-energy profiles are given in Figures 1S and
 506 2S, and those for the other three pathways are given in Figures
 507 3S and 4S in the Supporting Information.

508 The product preceded by **TS- β -ethox** is Ni₃O(OH)₂ and
 509 ethylene. The product preceded by **TS- α -ethox** is an adsorbing
 510 acetaldehyde, as proposed elsewhere.³⁶ The product preceded
 511 by **TS-cle-ethox** is methylnickel and an adsorbing form-
 512 aldehyde molecule. By putting the free-energy profiles depicted
 513 in Figures 2S and 4S together, one can see that for **Ethoxide-1**
 514 the most easily undergoing pathway is C–C bond cleavage, and
 515 the second most easily undergoing one is to isomerize to
 516 **Ethynickel-2**. This is dramatically different from the reaction
 517 behavior of **Ethynickel-1**. The relative rate of these two
 518 pathways $k_{\text{iso-2}}/k_{\text{cle}} = 0.15$ using eq 1. The β -H elimination
 519 pathway of ethoxide to afford ethylene is a much slower process
 520 as $k_{\beta}/k_{\text{cle}} = 4.3 \times 10^{-4}$. The reaction rate of the α -H abstraction
 521 pathway is even lower. The above data show that when an
 522 ethoxide intermediate is formed, it is unlikely to produce
 523 ethylene (with β -H elimination pathway).

524 **3.3. Ethylene Selectivity for C₂H₆ Reacting with Ni₃O₃.**
 525 Putting together all free-energy profiles in Sections 3.1 and 3.2,
 526 the selectivity of ethylene (S_{C_2}) can be calculated for the
 527 reaction of C₂H₆ with Ni₃O₃ cluster. In Section 3.1, it has been
 528 demonstrated that producing **Ethynickel-1** is a main pathway
 529 for the C–H bond activation step. In Section 3.2, it has been

demonstrated that **Ethynickel-1** may undergo four reaction
 530 pathways, α -H abstraction, β -H elimination, C–C bond
 531 cleavage, and isomerization to form **Ethoxide-1**. The result
 532 described in Section 3.2.5 shows that if **Ethynickel-1** is
 533 converted to **Ethoxide-1**, then it is not likely to form ethylene.
 534 Therefore, the sum of rate constants of all pathways that
 535 produce ethylene, denoted as k_{A} , equals k_{β} , and the sum of rate
 536 constants of all pathways that do not produce ethylene,
 537 denoted as k_{B} , equals $k_{\alpha} + k_{\text{cle}} + k_{\text{iso-1}}$. Then, S_{C_2} for C₂H₆
 538 reacting with Ni₃O₃ cluster can be calculated by
 539

$$\begin{aligned}
 S_{\text{C}_2} &= k_{\text{A}} / (k_{\text{A}} + k_{\text{B}}) \\
 &= \frac{k_{\beta}}{k_{\beta} + k_{\alpha} + k_{\text{cle}} + k_{\text{iso-1}}} \\
 &= [\exp(-G_{\text{TS-}\beta}/RT)] / [\exp(-G_{\text{TS-}\beta}/RT) \\
 &\quad + \exp(-G_{\text{TS-}\alpha}/RT) + \exp(-G_{\text{TS-cle}}/RT) \\
 &\quad + \exp(-G_{\text{TS-iso-1}}/RT)] \quad (2)
 \end{aligned}$$

where G_{TS} is the free energy for a transition state relative to an
 540 arbitrary reference. When $T = 873.15$ K, S_{C_2} is calculated to be
 541 37.0%, which is 36.2% at 823.15 K upon employing eq 2. The
 542 G_{TS} data for all four pathways examined for **Ethynickel-1** can
 543 be seen in Figures 5b and 7. The relatively low selectivity of
 544 ethylene is mainly due to a slightly higher $G_{\text{TS-}\beta-1}$ than $G_{\text{TS-iso-1}}$.
 545 The contribution of the α -H abstraction pathway is small
 546 compared with that of the β -H elimination pathway, as $k_{\alpha}/k_{\beta} =$
 547 0.047 at 873.15 K, and the contribution of the C–C bond
 548 cleavage pathway is unlikely to undergo, as $k_{\text{cle}}/k_{\beta} = 1.8 \times 10^{-7}$
 549 at 873.15 K.
 550

551 **3.4. C₂H₆ Reacting with Ni₃O₂ and Ni₃O₁ Clusters.** The
 552 Ni₃O₂ and Ni₃O₁ clusters were used in this work to model the
 553 active sites when exposed to the reaction feed with a fuel-rich
 554 atmosphere. (The flow rate of C₂H₆ is larger than that of O₂ for
 555 ODHE for instance.)^{31–41} The reactions of C₂H₆ with Ni₃O₂
 556 and Ni₃O₁ were investigated by examination of similar reaction
 557 steps and pathways, as examined for the reaction of C₂H₆ with
 558 Ni₃O₃. The primary reaction pathway for the C–H bond
 559 activation step (first step) and the primary reaction channel for
 560 different pathways in the second step for both of these two
 561 reactions are indicated in Scheme 2. The optimized geometries
 562 of the species involved in Scheme 2 are presented in Figures 5S
 563 and 6S in the Supporting Information.

564 For the C–H bond activation step undergoing with a
 565 concerted mechanism on an Ni₃O₂ cluster, C(1) may be bound
 566 to either Ni(1) or Ni(2) site, as indicated in Figure 1b. It was
 567 found that the reaction channel with lower free energy of
 568 activation for the C–H bond activation is to undergo with the
 569 Ni(1) site (Scheme 2a and the left two panels in Figure 5S in
 570 the Supporting Information). The product for the C–H bond
 571 activation step is denoted as **Ethynickel-Ni₃O₂**. In the second
 572 step, **Ethynickel-Ni₃O₂** may undergo four pathways, the same
 573 as those described in the **Ethynickel-1** case (Scheme 1). Figure
 574 10 depicts the corresponding free-energy profiles for the first
 575 and second steps. It can be seen that the free energy of the
 576 transition state for the β -H elimination pathway is slightly

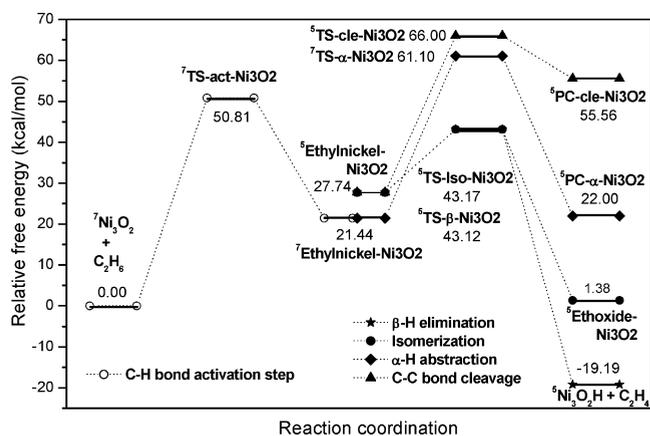


Figure 10. Free-energy profiles (at 873.15 K) for the C–H bond activation step (○), and four pathways after the C–H bond activation step for β -H elimination (★), α -H elimination (◆), C–C bond cleavage (▲), and isomerization (●), for C₂H₆ reacting with Ni₃O₂. Note that the free energies of TSs for β -H elimination and isomerization are so close to each other that the corresponding lines are nearly overlapped with each other.

577 smaller than that for the isomerization pathway, and those for
 578 α -H elimination and C–C bond cleavage pathways are much
 579 larger.

580 The C–H bond activation step (Scheme 2b and the left two
 581 panels in Figure 6S in the Supporting Information) undergoes a
 582 similar mechanism as in the cases of Ni₃O₃ and Ni₃O₂. The
 583 product of this step is denoted as **Ethynickel-Ni₃O₁**. The free
 584 energy of activation (46.2 kcal/mol at 873.15 K, see Figure 11)
 585 for the Ni₃O₁ case is slightly less than those in the cases of
 586 Ni₃O₃ (47.1 kcal/mol) and Ni₃O₂ (50.8 kcal/mol). For the
 587 second step, because there is no “bare” O atom in the neighbor
 588 of the C₂H₅ moiety of **Ethynickel-Ni₃O₁**, the isomerization
 589 pathway to afford ethoxide species is unlikely and thus is not

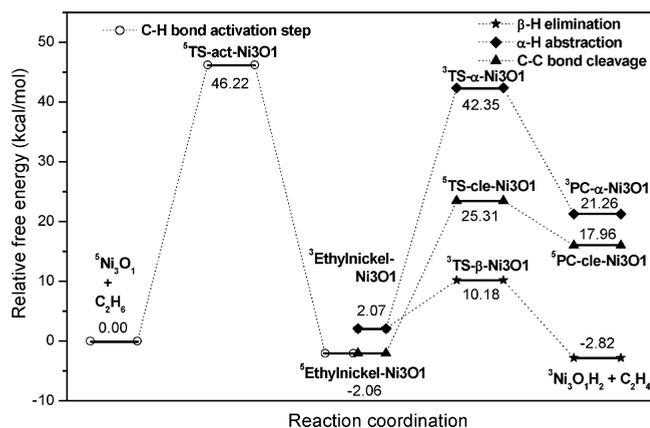


Figure 11. Free-energy profiles (at 873.15 K) for the C–H bond activation step (in open circles) and three pathways after the C–H bond activation step for β -H elimination (★), α -H elimination (◆), and C–C bond cleavage (▲) for C₂H₆ reacting with Ni₃O₁.

considered here, and the β -H and α -H atoms cannot go to an
 O(2) site like those in Ni₃O₃ and Ni₃O₂ cases. Therefore, the
 reaction channel of the β -H elimination pathway likes the
 CHAN- β -6 in the Ni₃O₃ case. (See $p = 6$ in Scheme 1a and in
 Figure 4.) The reaction channel of the α -H abstraction pathway
 likes the CHAN- α -6 in the Ni₃O₃ case. (See $p = 6$ in Scheme
 1b and in Figure 6.) Figure 11 also depicts the free-energy
 profiles for these three reaction pathways. It can be seen that
 the reaction barrier required by β -H elimination is much less
 than those for the α -H abstraction and C–C bond cleavage
 pathways.

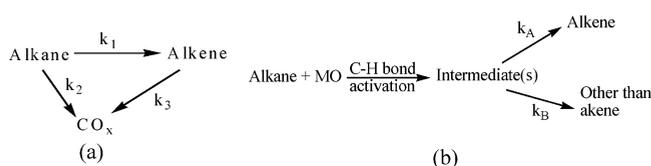
By applying the free-energy data for these two reaction
 (Figures 10 and 11) to eq 2, one can obtain the selectivity of
 ethylene (S_{C_2}) for both reactions. The S_{C_2} is 50.7% at 873.15 K
 and 50.5% at 823.15 K for C₂H₆ reacting with Ni₃O₂. The
 increase in S_{C_2} for the Ni₃O₂ case compared with the Ni₃O₃
 case is accounted for the increase in relative reaction rate of the
 β -H elimination pathway over the isomerization pathway. For
 the case of C₂H₆ reacting with Ni₃O₁, the contributions of α -H
 abstraction and C–C bond cleavage are trivial, as $k_{\alpha}/k_{\beta} = 8.9 \times$
 10^{-9} and $k_{cle}/k_{\beta} = 4.7 \times 10^{-4}$, and the absence of isomerization
 leads to very high S_{C_2} of >99%.

3.5. Further Discussion on the Mechanism and Catalyst Design For ODH Reaction of Alkanes. Sections 3.1–3.4 present a detailed structural and energetic investigation for the reactions of C₂H₆ with Ni₃O_x ($x = 1, 2, 3$) clusters, which model the small NiO·Ni_y clusters³⁶ in a supported catalyst with different oxidation states of nickel element. By inspection of all free-energy profiles in this Article (Figures 3, 5, 7, 10, and 11 and Figures 2S and 4S of the Supporting Information), one may find that the free energy of activation required by the first step is higher than that by the second step for all cases of different x values, indicating that the first step is rate-determining according to the energetic span model.^{59–61} However, the second step determines the product selectivity instead of the first step. The selectivity of ethylene calculated by employing eq 2 for a certain reaction increases from 37.0% when $x = 3$ to 50.7% when $x = 2$ and to over 99% when $x = 1$. The increasing S_{C_2} mainly accounts for the increase in relative rate of the β -H elimination pathway over the isomerization pathway. This implicates, that the reaction behavior of the intermediate produced from the first step as well as the selectivity of ethylene is sensitively dependent on the oxidation

state of the active sites. A more reduced state of the nickel component may benefit the production of alkene for the ODH reactions. An ideal ODH catalyst could have a high concentration of active sites that produce alkylmetal species in the first step and block the isomerization pathway in the second step.

In our previous study, we have found that on the zeolite-Y supported nickel oxide catalyst³⁵ the initial selectivity of ethylene (S_0) from the ethane oxidation ranges from 90 to 96% at the temperature of 550–600 °C. S_0 was obtained from the plot of the selectivity to ethylene with the conversion of ethane by the extrapolation of the conversion to 0. According to the generally accepted reaction scheme (Scheme 3a)^{5,57} for ODH reactions, the selectivity of alkene at low conversion of alkane mainly depends on the k_1/k_2 ratio, whereas at higher conversions of alkane, the observed selectivity of alkene is

Scheme 3. Simple Reaction Networks of Oxidative Dehydrogenation of Alkanes to Alkenes: (a) General Scheme and (b) Initial Steps in the Mars–van Krevelen Mechanism



associated with the ratio $k_1/(k_2 + k_3)$. When the conversion is extrapolated to 0, the corresponding selectivity can be calculated as: $S_0 = k_1/(k_1 + k_2)$. However, on the molecular level, the conversion of alkane either to alkene or to CO_x may contain several steps that are not well understood.

The ODH catalysts can be divided into three categories,⁸ that is, (1) catalysts based on reducible metal oxides, (2) noble-metal-based catalysts, primarily Pt-based ones, and (3) catalysts that generate radicals to initiate homogeneous reactions in the gas phase. (These are typically alkali earth and rear earth metal oxides.) The first category is the most extensively studied, and the reaction mechanism is generally believed to be the Mars–van Krevelen mechanism involving a key step of C–H bond activation.² As illustrated in Scheme 3b, if the primary intermediate of the C–H bond activation step is known, then k_1/k_2 is associated with the relative rate of the pathways that produce alkene and that do not produce alkene, or $k_1/k_2 = k_A/k_B$. (See Section 3.3.) Therefore, S_0 should be equal to S_{C_2} (eq 2) if only one type of active site exists in the supported catalyst. However, there can be various types of active site on a common catalyst even if there is only one type of metal in the active component. The experimental data³⁵ implicate that, more than 90% of the intermediate(s) from the C–H bond activation step is converted to ethylene, and a small portion is converted to species other than ethylene. The computational result in this work shows that the selectivity of ethylene is highly dependent on the degree of reduction of the metal oxide clusters. Therefore, it is reasonable to anticipate that in the real catalyst the C–H bond activation mainly undergoes on a relatively more reduced site rather than on more oxidized sites. This is consistent with the result that the free energy of activation needed for the C–H bond activation step in the Ni_3O_1 case is lower than those in the Ni_3O_2 and Ni_3O_3 cases. (See Figures 3, 10, and 11.)

Because of high demand of the computational resource in calculating metal oxide nanoclusters with different spin multiplicity, the incorporation of a support into the Ni_3O_x clusters was not examined in this Article. However, because support effect is also important to the catalytic performance of a catalyst, a further DFT study of the support effect is desirable for a deeper understanding of the ODH mechanism. The work along this avenue is now being performed in our group.

4. CONCLUSIONS

The following conclusions on the reactions of C_2H_6 with Ni_3O_x ($x = 1, 2, 3$) clusters can be made:

- (1) For the case of Ni_3O_3 , the C–H bond activation step may undergo with three pathways, with concerted or stepwise mechanisms. The pathway with concerted mechanism where the C and H atoms on the C–H bond attack two different sites is the most favorable pathway. The main product produced from the C–H bond activation step is **Ethylnickel-1**.
- (2) Eleven reaction channels were examined to understand the reaction behavior of **Ethylnickel-1**: five for the β -H elimination pathways to afford ethylene, three for the α -H abstraction pathway, two for the C–C bond cleavage pathway, and one for the isomerization pathway to produce **Ethoxide-1**. The most favorable two pathways are isomerization and β -H elimination.
- (3) The most favorable pathway for **Ethoxide-1** is to undergo C–C bond cleavage, resulting in a situation that if **Ethylnickel-1** undergoes isomerization pathway, then ethylene is unlikely to be produced. The selectivity of ethylene (S_{C_2}) can be calculated from the relative rate of β -H elimination over the sum of rates for all pathways for **Ethylnickel-1**.
- (4) S_{C_2} for C_2H_6 reacting with Ni_3O_3 is $\sim 37\%$, which is slightly over 50% for the Ni_3O_2 case and is over 99% for the Ni_3O_1 case at 823–873 K. The high S_{C_2} for the Ni_3O_1 case is due to the absence of bare O atom nearby the α -Ni site, which makes the isomerization pathway unavailable.

This work provides a deep insight into the reaction mechanism for ODH reactions catalyzed by Ni-based catalysts. The conclusion that S_{C_2} increases with decreasing x value in the Ni_3O_x cluster may provide an important clue for designing ODH catalysts giving high ethylene selectivity.

■ ASSOCIATED CONTENT

Supporting Information

Optimized geometries, relative free energies, and Cartesian coordinates for all the optimized structures at the B3LYP/BS1 level of theory in the manuscript. This material is available free of charge via the Internet at <http://pubs.acs.org>.

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